## Name

eqn - format equations for groff or MathML

## Synopsis

eqn $[-\mathbf{C N r R}][-\mathrm{d} x y][-\mathbf{f} F][-\mathbf{m} n][-\mathbf{M} \operatorname{dir}][-\mathbf{p} n][-\mathbf{s} n][-\mathbf{T}$ name $][$ file $\ldots]$
eqn --help
eqn -v
eqn --version

## Description

The GNU implementation of eqn is part of the groff(7) document formatting system. eqn is a troff(1) preprocessor that translates descriptions of equations embedded in roff (7) input files into the language understood by troff (1). It copies the contents of each file to the standard output stream, except that lines between .EQ and .EN (or within a pair of user-specified delimiters) are interpreted as equation descriptions. Normally, eqn is not executed directly by the user, but invoked by specifying the $\mathbf{- e}$ option to $\operatorname{groff}$ (1). While GNU eqn's input syntax is highly compatible with AT\&T eqn, the output eqn produces cannot be processed by AT\&T troff; GNU troff (or a troff implementing relevant GNU extensions) must be used. If no file operands are given on the command line, or if file is "-", eqn reads the standard input stream.

Unless the $\mathbf{- R}$ option is given, eqn searches for the file eqnrc in the directories given with the $\mathbf{-} \mathbf{M}$ option first, then in /usr/local/share/groff/site-tmac, and finally in the standard macro directory /usr/local/share/ groff/1.23.0/tmac. If it exists and is readable, eqn processes it before any input files.
This man page primarily discusses the differences between GNU eqn and AT\&T eqn. Most of the new features of the GNU eqn input language are based on $\mathrm{T}_{\mathrm{E}} \mathrm{X}$. There are some references to the differences between $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ and GNU eqn below; these may safely be ignored if you do not know $\mathrm{T}_{\mathrm{E}} \mathrm{X}$.

Three points are worth special note.

- GNU eqn emits Presentation MathML output when invoked with the "-T MathML" option.
- GNU eqn does not provide the functionality of neqn: it does not support low-resolution, typewriter-like devices (although it may work adequately for very simple input).
- GNU eqn sets the input token "..." as three periods or low dots, rather than the three centered dots of AT\&T eqn. To get three centered dots, write cdots or "cdot cdot cdot".


## Anatomy of an equation

eqn input consists of tokens. Consider a form of Newton's second law of motion. The input

$$
\begin{aligned}
& . \mathrm{EQ} \\
& \mathrm{~F}= \\
& \mathrm{m} a \\
& . \mathrm{EN}
\end{aligned}
$$

becomes $F=m a$. Each of $\mathbf{F},=, \mathbf{m}$, and $\mathbf{a}$ is a token. Spaces and newlines are interchangeable; they separate input tokens but do not break lines or produce space in the output.

A handful of tokens manage the grouping and spacing of other tokens.
\{ \} Braces perform grouping. Whereas "e sup ab" expresses $e^{a} b$, "e sup \{ab\}" means $e^{a b}$.
~ are the half space and full space, respectively. Use them to tune the appearance of the output.
Tab and leader characters separate tokens as well as advancing the drawing position to the next tab stop, but are seldom used in eqn input. When they occur, they must appear at the outermost lexical scope. This roughly means that they can't appear within braces that are necessary to disambiguate the input; eqn will diagnose an error in this event.

Other tokens are primitives, macros, an argument to either of the foregoing, or a component of an equation.
Primitives are fundamental keywords of the eqn language. They can configure an aspect of the preprocessor's state, as when setting a "global" font selection or type size (gfont and gsize), or declaring or deleting
macros (define and undefine); these are termed commands. Other primitives perform formatting operations on the tokens after them (as with fat, over, sqrt, or up).

Macros permit primitives and/or components of equations to be grouped together for convenience. Predefined macros make convenient the preparation of eqn input in a form resembling its spoken expression; for example, consider cos, hat, inf, and lim.

Equation components include mathematical variables, constants, numeric literals, and operators. eqn remaps some input character sequences for convenience in equation entry and to ensure that glyphs from an unstyled font are used; see groff_char(7).

```
+ \[pl]
- \[mi]
= \[eq]
' \[fm]
<= \[<=]
>= \[>=]
```


## Spacing and typeface

GNU eqn imputes types to the components of an equation, adjusting the spacing between them accordingly.
Recognized types are as follows; most affect spacing only, whereas the "letter" subtype of "ordinary" also assigns a style.

```
ordinary character such as "1", "a", or "!"
    letter character to be italicized by default
    digit n/a
operator large operator such as " }\sum\mathrm{ "
binary binary operator such as "+"
relation relation such as "="
opening opening bracket such as "("
closing closing bracket such as ")"
punctuation punctuation character such as ","
inner sub-formula contained within brackets
suppress component to which automatic spacing is not applied
```

Two primitives apply types to equation components.
type $t e$ Apply type $t$ to expression $e$.
chartype $t$ text
Assign each character in (unquoted) text type $t$, persistently.
eqn sets up spacings and styles as if by the following commands.

```
chartype "letter" abcdefghiklmnopqrstuvwxyz
chartype "letter" ABCDEFGHIKLMNOPQRSTUVWXYZ
chartype "letter" \[*a]\[*b]\[*x]\[*d]\[*e]\[*y]
chartype "letter" \[*g]\[*i]\[*k]\[*l]\[*m]\[*n]
chartype "letter" \[*w]\[*o]\[*f]\[*p]\[*q]\[*r]
chartype "letter" \[*s]\[*t]\[*h]\[*u]\[*c]\[*z]
chartype "binary" *\[pl]\[mi]
chartype "relation" <>\[eq]\[<=]\[>=]
chartype "opening" {([
chartype "closing" })]
chartype "punctuation" ,;:.
chartype "suppress" ^~
```

eqn assigns all other ordinary and special roff characters, including numerals $0-9$, the "ordinary" type. (The "digit" type is not used, but is available for customization.) In keeping with common practice in mathematical typesetting, lowercase, but not uppercase, Greek letters are assigned the "letter" type to style them in italics.

## Primitives

eqn supports without alteration the AT\&T eqn primitives above, back, bar, bold, define, down, fat, font, from, fwd, gfont, gsize, italic, left, lineup, mark, matrix, ndefine, over, right, roman, size, sqrt, sub, sup, tdefine, to, under, and up.

## New primitives

The GNU extension primitives "type" and chartype are discussed in subsection "Spacing and typeface" above; "set" in subsection "Customization" below; and grfont and gbfont in subsection "Fonts" below.
big $e \quad$ Enlarges the expression $e$; intended to have semantics like CSS "large". In troff output, the type size is increased by 5 . MathML output emits the following.

```
<mstyle mathsize='big'>
```

e1 smallover $e 2$

This is similar to over; smallover reduces the size of $e 1$ and $e 2$; it also puts less vertical space between $e l$ or $e 2$ and the fraction bar. The over primitive corresponds to the $\mathrm{T}_{\mathrm{E}} \mathrm{X}$ lover primitive in displayed equation styles; smallover corresponds to \over in non-display ("inline") styles.

## vcenter $e$

This vertically centers $e$ about the math axis. The math axis is the vertical position about which characters such as " + " and "-" are centered; it is also the vertical position used for fraction bars. For example, sum is defined as follows.

```
{ type "operator" vcenter size +5 \(*S }
```

vcenter is silently ignored when generating MathML.

## $e 1$ accent $e 2$

This sets $e 2$ as an accent over $e 1 . e 2$ is assumed to be at the correct height for a lowercase letter; $e 2$ is moved down according to whether el is taller or shorter than a lowercase letter. For example, hat is defined as follows.

```
accent { "^" }
```

dotdot, dot, tilde, vec, and dyad are also defined using the accent primitive.
$e 1$ uaccent $e 2$
This sets $e 2$ as an accent under $e 1 . e 2$ is assumed to be at the correct height for a character without a descender; $e 2$ is moved down if $e l$ has a descender. utilde is predefined using uaccent as a tilde accent below the baseline.
split "text"
This has the same effect as simply

```
text
```

but text is not subject to macro expansion because it is quoted; text is split up and the spacing between individual characters adjusted per subsection "Spacing and typeface" above.
nosplit text
This has the same effect as
"text"
but because text is not quoted it is subject to macro expansion; text is not split up and the spacing between individual characters not adjusted per subsection "Spacing and typeface" above.

## $e$ opprime

This is a variant of prime that acts as an operator on $e$. It produces a different result from prime in a case such as "A opprime sub 1": with opprime the " 1 " is tucked under the prime as a subscript to the " A " (as is conventional in mathematical typesetting), whereas with prime the " 1 " is a subscript to the prime character. The precedence of opprime is the same as that of bar and under, which is higher than that of everything except accent and uaccent. In unquoted text, a neutral apostrophe (') that is not the first character on the input line is treated like opprime.

## special troff-macro e

Construct an object by calling troff-macro on $e$. The troff string 0 s contains the eqn output for $e$, and the registers $\mathbf{0 w}, \mathbf{0 h}, \mathbf{0 d}, \mathbf{0} \mathbf{s k e r n}$, and 0skew the width, height, depth, subscript kern, and skew of $e$, respectively. (The subscript kern of an object indicates how much a subscript on that object should be "tucked in", or placed to the left relative to a non-subscripted glyph of the same size. The skew of an object is how far to the right of the center of the object an accent over it should be placed.) The macro must modify $\mathbf{0 s}$ so that it outputs the desired result, returns the drawing position to the text baseline at the beginning of $e$, and updates the foregoing registers to correspond to the new dimensions of the result.

Suppose you want a construct that "cancels" an expression by drawing a diagonal line through it.

```
.de Ca
. ds 0s \
\'\\*(0s'\
\v'\\n(0du'\
\D'l \\n(Owu -\\n(Ohu-\\n(Odu'\
\v'\\n(Ohu'
.EQ
special Ca "x \[mi] 3 \[pl] x" ~ 3
.EN
```

We use the $\backslash[\mathbf{m i}]$ and $\backslash[\mathbf{p l}]$ special characters instead of + and - because they are part of the argument to a troff macro, so eqn does not transform them to mathematical glyphs for us. Here's a more complicated construct that draws a box around an expression; the bottom of the box rests on the text baseline. We define the eqn macro box to wrap the call of the troff macro $\mathbf{B x}$.

```
.de Bx
.ds 0s \
\Z'\\h'1n'\\*[0s]'\
\v'\\n(0du+1n'\
\D'l \\n(Owu+2n 0'\
\D'l 0 -\\n(0hu-\\n(0du-2n'\
\D'l -\\n(Owu-2n 0'\
\D'l 0 \\n(Ohu+\\n(Odu+2n'\
\h'\\n(0wu+2n'
.nr 0w +2n
.nr Od +1n
.nr Oh +1n
.EQ
define box ' special Bx $1 '
box(foo) ~ "bar"
.EN
```

space $n$
Set extra vertical spacing around the equation, replacing the default values, where $n$ is an integer in hundredths of an em. If positive, $n$ increases vertical spacing before the equation; if negative, it does so after the equation. This primitive provides an interface to groff's $\backslash \mathbf{x}$ escape sequence, but with the opposite sign convention. It has no effect if the equation is part of a pic(1) picture.

## Extended primitives

eqn recognizes an "on" argument to the delim primitive specially, restoring any delimiters previously disabled with "delim off". If delimiters haven't been specified, neither command has effect.
$\boldsymbol{\operatorname { c o l }} n\{\ldots\}$
$\operatorname{ccol} n\{\ldots\}$
$\operatorname{lcol} n\{\ldots\}$
$\operatorname{rcol} n\{\ldots\}$
pile $n\{\ldots\}$
cpile $n\{\ldots\}$
lpile $n\{\ldots\}$
rpile $n\{\ldots\}$
The integer value $n$ (in hundredths of an em) increases the vertical spacing between rows, using groff's $\backslash \mathbf{x}$ escape sequence (the value has no effect in MathML mode). Negative values are accepted but have no effect. If more than one $n$ occurs in a matrix, the largest is used.

## Customization

When eqn generates troff input, the appearance of equations is controlled by a large number of parameters. They have no effect when generating MathML, which delegates typesetting to a MathML rendering engine. Configure these parameters with the set primitive.
set $p n$ assigns parameter $p$ the integer value $n ; n$ is interpreted in units of hundredths of an em unless otherwise stated. For example,

```
set x_height 45
```

says that eqn should assume that the font's x -height is 0.45 ems .
Available parameters are as follows; defaults are shown in parentheses. We intend these descriptions to be expository rather than rigorous.
minimum_size sets a floor for the type size (in scaled points) at which equations are set (5).
fat_offset
The fat primitive emboldens an equation by overprinting two copies of the equation horizontally offset by this amount (4). fat_offset is not used in MathML mode; fat components use

```
    <mstyle mathvariant='double-struck'>
```

instead.
over_hang A fraction bar is longer by twice this amount than the maximum of the widths of the numerator and denominator; in other words, it overhangs the numerator and denominator by at least this amount (0).
accent_width When bar or under is applied to a single character, the line is this long (31). Normally, bar or under produces a line whose length is the width of the object to which it applies; in the case of a single character, this tends to produce a line that looks too long.
delimiter_factor Extensible delimiters produced with the left and right primitives have a combined height and depth of at least this many thousandths of twice the maximum amount by which the sub-equation that the delimiters enclose extends away from the axis (900).
delimiter_shortfall Extensible delimiters produced with the left and right primitives have a combined height and depth not less than the difference of twice the maximum amount by which the sub-equation that the delimiters enclose extends away from the axis and this amount (50).
null_delimiter_space
This much horizontal space is inserted on each side of a fraction (12).

| script_space | width of subscripts and superscripts is increased by this amount (5). |
| :---: | :---: |
| thin_space | This amount of space is automatically inserted after punctuation characters. It also configures the width of the space produced by the ${ }^{\wedge}$ token (17). |
| medium_space | This amount of space is automatically inserted on either side of binary operators (22). |
| thick_space | This amount of space is automatically inserted on either side of relations. It also configures the width of the space produced by the $\sim$ token (28). |
| x_height | The height of lowercase letters without ascenders such as " x " (45). |
| axis_height | The height above the baseline of the center of characters such as " + " and "-" (26). It is important that this value is correct for the font you are using. |
| default_rule_thickness |  |
|  | This should be set to the thickness of the $\backslash \mathbf{r u}]$ character, or the thickness of horizontal lines produced with the $\backslash \mathbf{D}$ escape sequence (4). |
| num1 | The over primitive shifts up the numerator by at least this amount (70). |
| num2 | The smallover primitive shifts up the numerator by at least this amount (36). |
| denom1 | The over primitive shifts down the denominator by at least this amount (70). |
| denom2 | The smallover primitive shifts down the denominator by at least this amount (36). |
| sup1 | Normally superscripts are shifted up by at least this amount (42). |
| sup2 | Superscripts within superscripts or upper limits or numerators of smallover fractions are shifted up by at least this amount (37). Conventionally, this is less than sup1. |
| sup3 | Superscripts within denominators or square roots or subscripts or lower limits are shifted up by at least this amount (28). Conventionally, this is less than sup2. |
| sub1 | Subscripts are normally shifted down by at least this amount (20). |
| sub2 | When there is both a subscript and a superscript, the subscript is shifted down by at least this amount (23). |
| sup_drop | The baseline of a superscript is no more than this much below the top of the object on which the superscript is set (38). |
| sub_drop | The baseline of a subscript is at least this much below the bottom of the object on which the subscript is set (5). |
| big_op_Spacing1 | The baseline of an upper limit is at least this much above the top of the object on which the limit is set (11). |
| big_op_Spacing2 | The baseline of a lower limit is at least this much below the bottom of the object on which the limit is set (17). |
| big_op_Spacing3 | The bottom of an upper limit is at least this much above the top of the object on which the limit is set (20). |
| big_op_spacing4 | The top of a lower limit is at least this much below the bottom of the object on which the limit is set ( $\mathbf{6 0}$ ). |
| big_op_spacing5 | This much vertical space is added above and below limits (10). |


| baseline_sep | The baselines of the rows in a pile or matrix are normally this far apart (140). Usually equal to the sum of num1 and denom1. |
| :---: | :---: |
| shift_down | The midpoint between the top baseline and the bottom baseline in a matrix or pile is shifted down by this much from the axis (26). Usually equal to axis_height. |
| column_sep | This much space is added between columns in a matrix (100). |
| matrix_side_sep | This much space is added at each side of a matrix (17). |
| draw_lines | If non-zero, eqn draws lines using the troff $\backslash \mathbf{D}$ escape sequence, rather than the $\backslash \mathbf{l}$ escape sequence and the $\backslash \mathbf{r u}]$ special character. The default is determined by the eqnrc file ( $\mathbf{0}$ on most devices; $\mathbf{1}$ on $\mathbf{p s}, \mathbf{h t m l}$, and the X11 devices.) |
| body_height | The amount by which the height of the equation exceeds this is added as extra space before the line containing the equation using the troff $\backslash \mathbf{x}$ escape sequence (85). |
| body_depth | The amount by which the depth of the equation exceeds this is added as extra space after the line containing the equation using the troff $\backslash \mathbf{x}$ escape sequence (35). |
| nroff | If non-zero, then ndefine behaves like define and tdefine is ignored, otherwise tdefine behaves like define and ndefine is ignored. The default is determined by the eqnrc file ( $\mathbf{0}$ on most devices; $\mathbf{1}$ on ascii, latin1, utf8, and cp1047). |

## Macros

In GNU eqn, macros can take arguments. In a macro body, $\$ n$, where $n$ is between 1 and 9 , is replaced by the $n$th argument if the macro is called with arguments; if there are fewer than $n$ arguments, it is replaced by nothing. A word containing a left parenthesis where the part of the word before the left parenthesis has been defined using the define primitive is recognized as a macro call with arguments; characters following the left parenthesis up to a matching right parenthesis are treated as comma-separated arguments. Commas inside nested parentheses do not terminate an argument. In the following synopses, $X$ can be any character not appearing in the parameter thus bracketed.
sdefine name $X$ anything $X$
This is like the define primitive, but name is not recognized if called with arguments.
include file
copy file
Interpolate the contents of file. Lines in file beginning with .EQ or .EN are ignored.

## ifdef name $X$ anything $X$

If name has been defined by define (or has been automatically defined because name is the output driver) process anything; otherwise ignore anything.
undef name
Remove definition of name, making it undefined.

## Predefined macros

GNU eqn supports the predefined macros offered by AT\&T eqn: and, approx, arc, cos, cosh, del, det, dot, dotdot, dyad, exp, for, grad, half, hat, if, inter, $\operatorname{Im}$, inf, int, lim, $\ln , \log$, max, min, nothing, partial, prime, prod, Re, sin, sinh, sum, tan, tanh, tilde, times, union, vec, ==, !=, +=, ->, <-, <<, >>, and "...". The lowercase classical Greek letters are available as alpha, beta, chi, delta, epsilon, eta, gamma, iota, kappa, lambda, mu, nu, omega, omicron, phi, pi, psi, rho, sigma, tau, theta, upsilon, xi, and zeta. Spell them with an initial capital letter (Alpha) or in full capitals (ALPHA) to obtain uppercase forms.
GNU eqn further defines the macros cdot, cdots, and utilde (all discussed above), dollar, which sets a dollar sign, and ldots, which sets three dots on the baseline.

## Fonts

eqn uses up to three typefaces to set an equation: italic (oblique), roman (upright), and bold. Assign each a groff typeface with the primitives gfont, grfont, and gbfont. The defaults are the styles $\mathbf{I}, \mathbf{R}$, and $\mathbf{B}$ (applied to the current font family). The chartype primitive (see above) sets a character's type, which determines the face used to set it. The "letter" type is set in italics; others are set in roman. Use the bold primitive to select an (upright) bold style.
gbfont $f$ Select $f$ as the bold font. This is a GNU extension.
gfont $f$
Select $f$ as the italic font.
grfont $f$
Select $f$ as the roman font. This is a GNU extension.

## Options

--help displays a usage message, while -v and --version show version information; all exit afterward.
-C Recognize .EQ and .EN even when followed by a character other than space or newline.
-d $x y \quad$ Specify delimiters $x$ for left and $y$ for right ends of equations not bracketed by .EQ/.EN. $x$ and $y$ need not be distinct. Any "delim $x y$ " statements in the source file override this option.
-f $F \quad$ is equivalent to "gfont $F$ ".
-m $n \quad$ is equivalent to "set minimum_size $n$ ".
-M dir Search dir for eqnrc before those listed in section "Description" above.
-N Prohibit newlines within delimiters. This option allows eqn to recover better from missing closing delimiters.
-p $n \quad$ Set sub- and superscripts $n$ points smaller than the surrounding text. This option is deprecated. eqn normally sets sub- and superscripts at $70 \%$ of the type size of the surrounding text.
$-\mathbf{r} \quad$ Reduce the type size of subscripts at most once relative to the base type size for the equation.
-R Don't load eqnrc.
-s $n \quad$ is equivalent to "gsize $n$ ". This option is deprecated. eqn normally sets equations at the type size current when the equation is encountered.
-T name
Prepare output for the device name. In most cases, the effect of this is to define a macro name with a value of $\mathbf{1}$; eqnrc uses this to provide definitions appropriate for the device. However, if the specified driver is "MathML", the output is MathML markup rather than troff input, and eqnrc is not loaded at all. The default output device is $\mathbf{p s}$.

## Files

/usr/local/share/groff/1.23.0/tmacleqnrc Initialization file.

## MathML mode limitations

MathML is designed on the assumption that it cannot know the exact physical characteristics of the media and devices on which it will be rendered. It does not support control of motions and sizes to the same degree troff does.

- eqn customization parameters have no effect on generated MathML.
- The special, up, down, fwd, and back primitives cannot be implemented, and yield a MathML "<merror>" message instead.
- The vcenter primitive is silently ignored, as centering on the math axis is the MathML default.
- Characters that eqn sets extra large in troff mode—notably the integral sign—may appear too small and need to have their "<mstyle>" wrappers adjusted by hand.

As in its troff mode, eqn in MathML mode leaves the .EQ and .EN tokens in place, but emits nothing corresponding to delim delimiters. They can, however, be recognized as character sequences that begin with "<math>", end with "</math>", and do not cross line boundaries.

## Caveats

Words must be quoted anywhere they occur in eqn input if they are not to be recognized as names of macros or primitives, or if they are to be interpreted by troff. These names, particularly short ones like "pi" and "PI", can collide with troff identifiers. For instance, the eqn command "gfont PI" does not select groff's Palatino italic font for the global italic face; you must use "gfont "PI"" instead.
Delimited equations are set at the type size current at the beginning of the input line, not that immediately preceding the opening delimiter.

Unlike $\mathrm{T}_{\mathrm{E}} \mathrm{X}$, eqn does not inherently distinguish displayed and inline equation styles; see the smallover primitive above. However, macro packages frequently define EQ and EN macros such that the equation within is displayed. These macros may accept arguments permitting the equation to labeled or captioned; see the package's documentation.

## Bugs

In nroff mode, lowercase Greek letters are rendered in roman instead of italic style.
In MathML mode, the mark and lineup features don't work. These could, in theory, be implemented with "<maligngroup>" elements.

In MathML mode, each digit of a numeric literal gets a separate "<mn></mn>" pair, and decimal points are tagged with "<mo></mo>". This is allowed by the specification, but inefficient.

## Examples

We first illustrate eqn usage with a trigonometric identity.

```
.EQ
sin ( alpha + beta ) = sin alpha cos beta + cos alpha sin beta
.EN
sin}(\alpha+\beta)=\operatorname{sin}\alpha\operatorname{cos}\beta+\operatorname{cos}\alpha\operatorname{sin}
```

It can be convenient to set up delimiters if mathematical content will appear frequently in running text.

```
.EQ
delim $$
.EN
With a large table of logarithms in memory,
we employed the property $ln ( x y ) = ln x + ln y$ to speed the
calculation.
```

With a large table of logarithms in memory, we employed the property $\ln (x y)=\ln x+\ln y$ to speed the calculation.

## See also

"Typesetting Mathematics-User's Guide" (2nd edition), by Brian W. Kernighan and Lorinda L. Cherry, 1978, AT\&T Bell Laboratories Computing Science Technical Report No. 17.
The $T_{E}$ Xbook, by Donald E. Knuth, 1984, Addison-Wesley Professional. Appendix G discusses many of the parameters from section "Customization" above in greater detail.
groff_char(7), particularly subsections "Logical symbols", "Mathematical symbols", and "Greek glyphs", documents a variety of special character escape sequences useful in mathematical typesetting.
groff (1), troff (1), pic(1), groff_font (5)

